

Time lags in evacuation in the social force model

Przemysław Gawroński, Krzysztof Kułakowski,
Jan Kantelhardt, Mirko Kämpf



Models of pedestrian behavior

- 1958 – Hankin & Wright – passengers flow in subway.
- 1970 – Henderson – Navier-Stokes equations approach to pedestrian flows.
- 1990 – Helbing – a pedestrian specific gas-kinetic (Boltzmann-like) model.
- 1995 – Helbing – a social forces model for pedestrian motion.
- 1997 – Schadschneider – cellular automaton model of pedestrian motion.
- 2003 – Kirchner – clogging in a cellular automaton model for pedestrian dynamics.

Models of pedestrian behavior

- All model quantities (places, velocities) are measurable and comparable with empirical data.
- Pedestrian models can provide valuable tools for designing and planning pedestrians area, subway, or rail-road stations, big buildings, shopping malls, etc.
- Analogies with gases and fluids – an extreme example of mechanistic reductionism.

Model of crowd dynamics

D. Helbing, I. Farkas and T. Vicsek „Simulating dynamical features of escape panic”, Nature **407**, 487-490, 2000

$$m_i \frac{d \vec{v}_i}{dt} = m_i \frac{v_i^0 \vec{e}_i^0(t) - \vec{v}_i(t)}{\tau} + \sum_{j(\neq i)} \vec{f}_{ij} + \sum_W \vec{f}_{iW}$$

m_i – mass of i – th pedestrian , **75kg**

v_i^0 – desired speed , **$3 \frac{m}{s}$**

$\vec{e}_i^0(t)$ – desired direction

$\vec{v}_i(t)$ – actual velocity

τ – acceleration time , **0.5s**

\vec{f}_{ij}, \vec{f}_W – 'interaction forces'

Model of crowd dynamics

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$$\vec{f}_{ij} = \left\{ A_i \exp\left(\frac{r_{ij} - d_{ij}}{B_i}\right) + k g(r_{ij} - d_{ij}) \right\} \vec{n}_{ij} + \kappa g(r_{ij} - d_{ij}) \Delta v_{ji}^t \vec{t}_{ij}$$

$$A_i = 2000 \text{ N}, B_i = 0.08 \text{ m}, k = 1.2 * 10^5 \frac{\text{kg}}{\text{s}^2}, \kappa = 2.4 * 10^5 \frac{\text{kg}}{\text{m s}}$$

\vec{r}_i = position of the i-th pedestrian

$d_{ij} = \|\vec{r}_i - \vec{r}_j\|$ – distance between the pedestrians

$\vec{n}_{ij} = (n_{ij}^1, n_{ij}^2) = \frac{\vec{r}_i - \vec{r}_j}{d_{ij}}$ – the normalized vector

pointing from j to i

$r_{ij} = (r_i + r_j)$ – sum of radii $r_i = 0.3 \text{ m}$ and $r_j = 0.3 \text{ m}$

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$$\vec{t}_{ij} = (-n_{ij}^2, n_{ij}^1) - \textit{tangential direction}$$

$$\Delta v_{ji}^t = (\vec{v}_j - \vec{v}_i) \cdot \vec{t}_{ij} - \textit{tangential velocity difference}$$

$$g(r_{ij} - d_{ij}) = \begin{cases} 0, & r_{ij} < d_{ij} \\ r_{ij} - d_{ij}, & r_{ij} \geq d_{ij} \end{cases}$$

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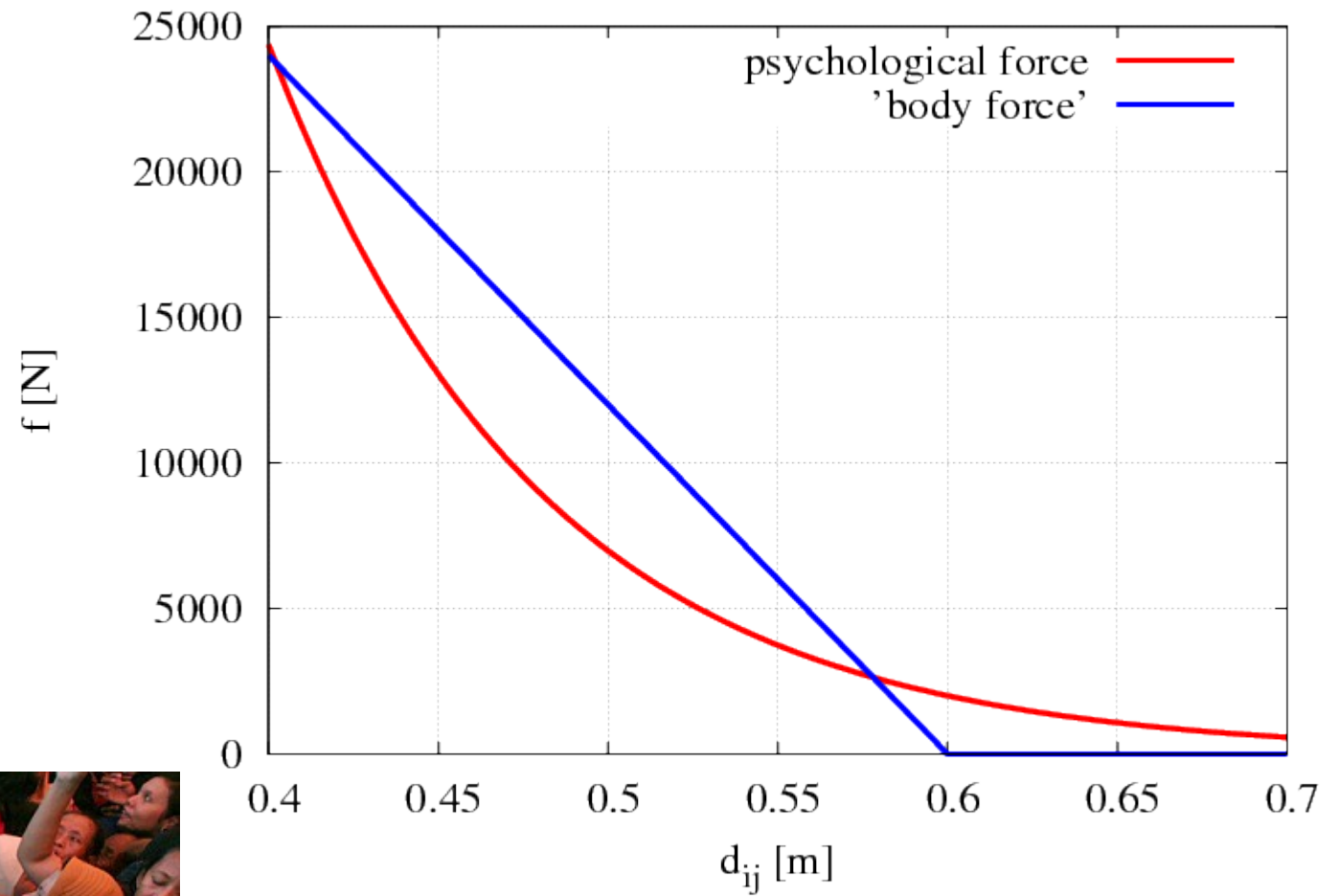
$$\vec{f}_{iW} = \left\{ A_i \exp\left(\frac{r_i - d_{iW}}{B_i}\right) + k g(r_i - d_{iW}) \right\} \vec{n}_{iW} \\ + \kappa g(r_i - d_{iW}) (\vec{v}_i \cdot \vec{t}_{iW}) \vec{t}_{iW}$$

d_{iW} – distance to wall W

\vec{n}_{iW} – direction perpendicular to wall W

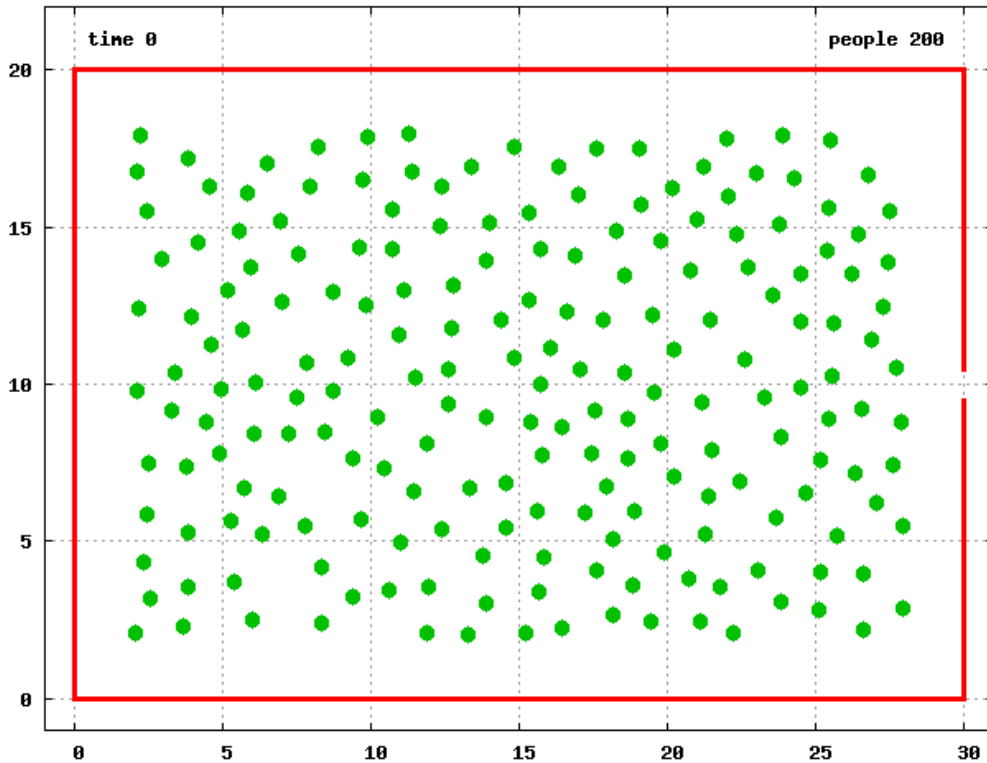
\vec{t}_{iW} – direction tangential to wall W

Simulation of crowd dynamics

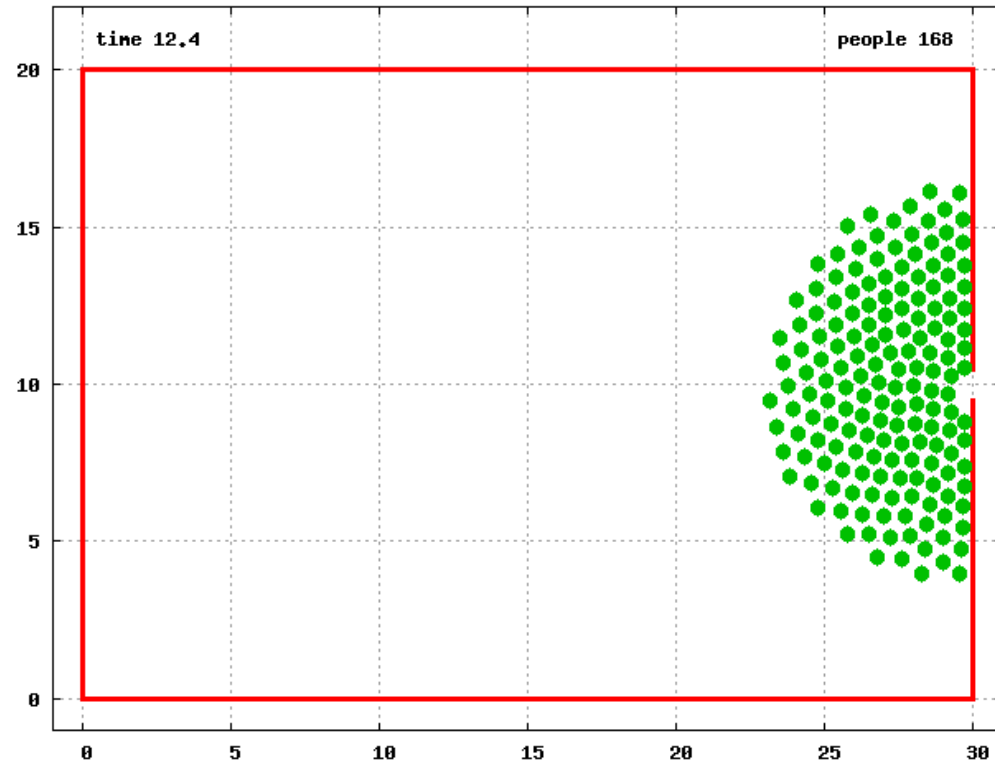


Simulation of crowd dynamics - snapshots

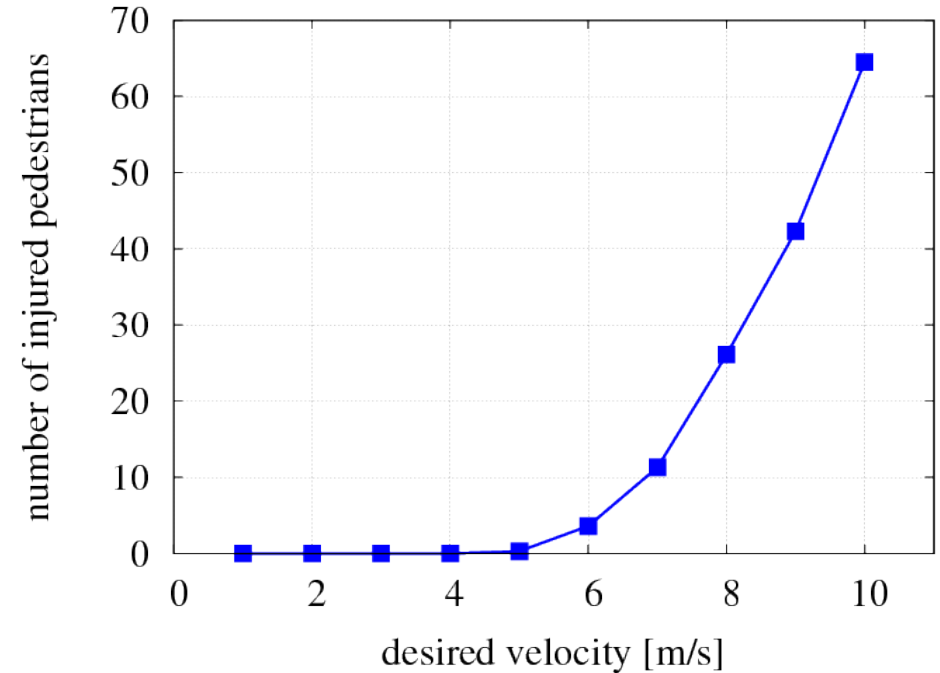
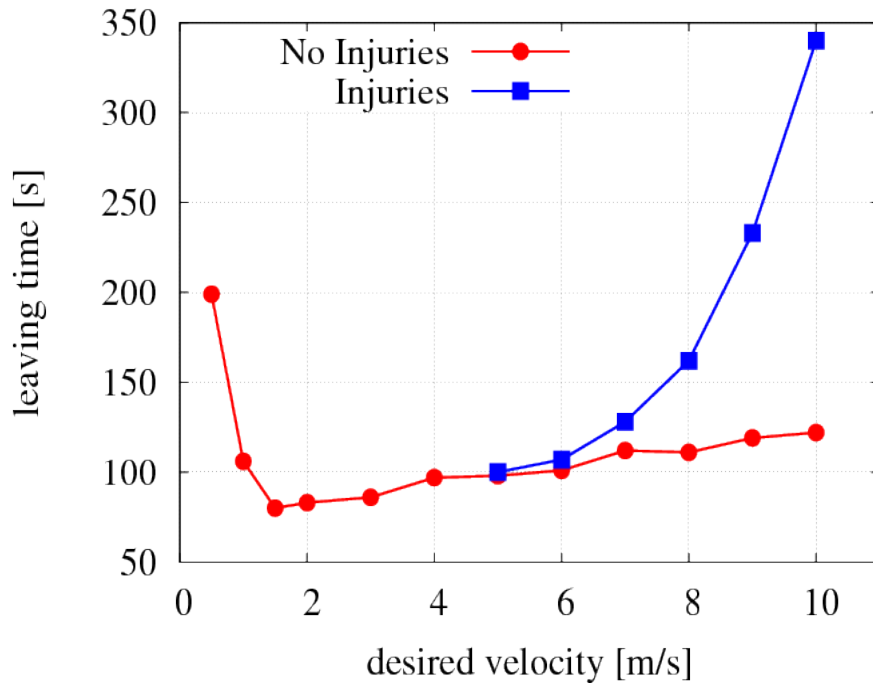
- initial state



- arch-like blocking of the exit



Simulation of crowd dynamics – 'faster-is-slower' effect



- Desired velocities $v_0 > 1.5 \text{ m/s}$ reduce the efficiency of leaving due to pushing, which causes additional friction effect.
- Above $v_0 = 5 \text{ m/s}$ pedestrians are injured if the pressure exceeds 1600 Nm^{-1} and become non-moving obstacles for others.

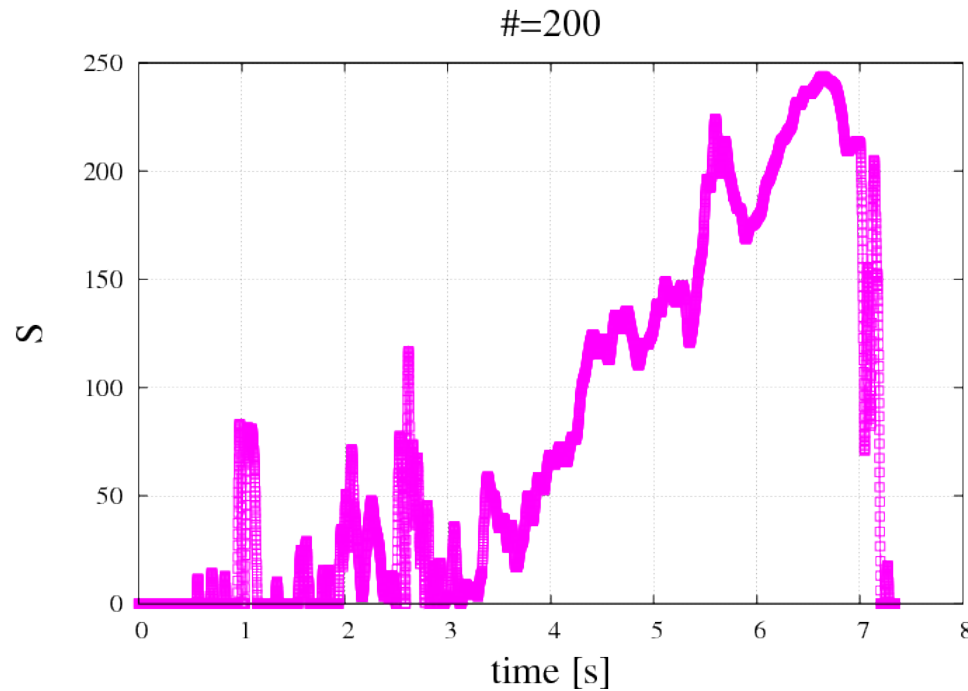
Is it possible to leave the crowd?



- The evidence from bent steel railings in several fatal crowd accidents have shown horizontal forces over 4500 N (equivalent to a weight of approximately 460 kg.)
- When the density of crowd becomes too large, pedestrians may die by e.g. compressive asphyxia.
- Before it happens **they might want to leave the crowd, but on what condition it is possible?**

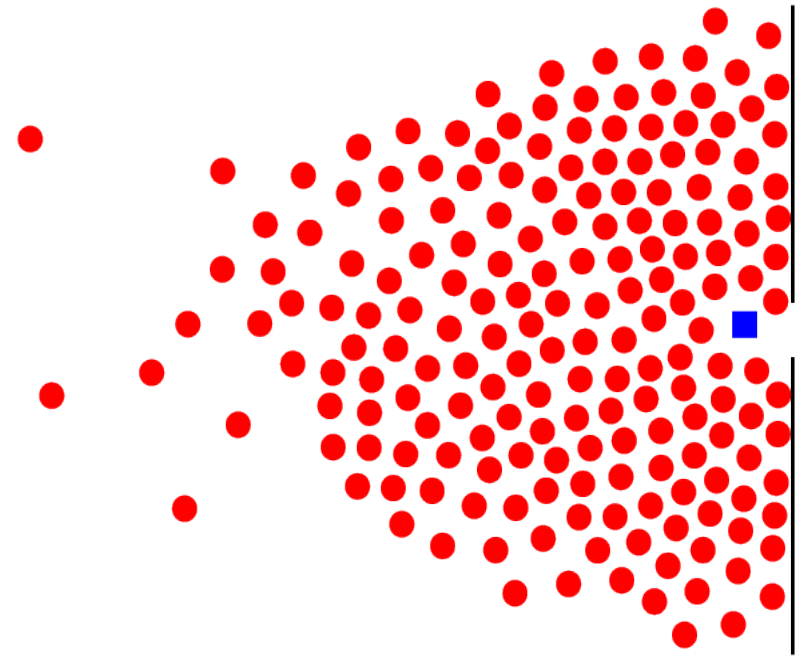
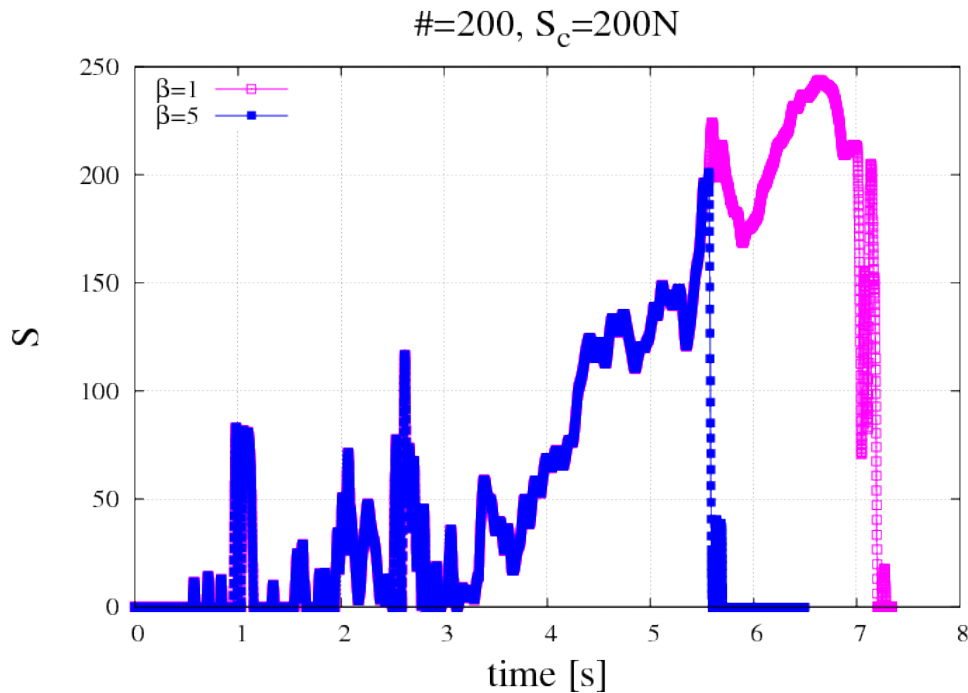
Is it possible to leave the crowd?

- S – sum of modules of the physical (not the psychological) compressive forces acting on pedestrians.
- S – a rough measure of pressure inconvenience in a crowd.



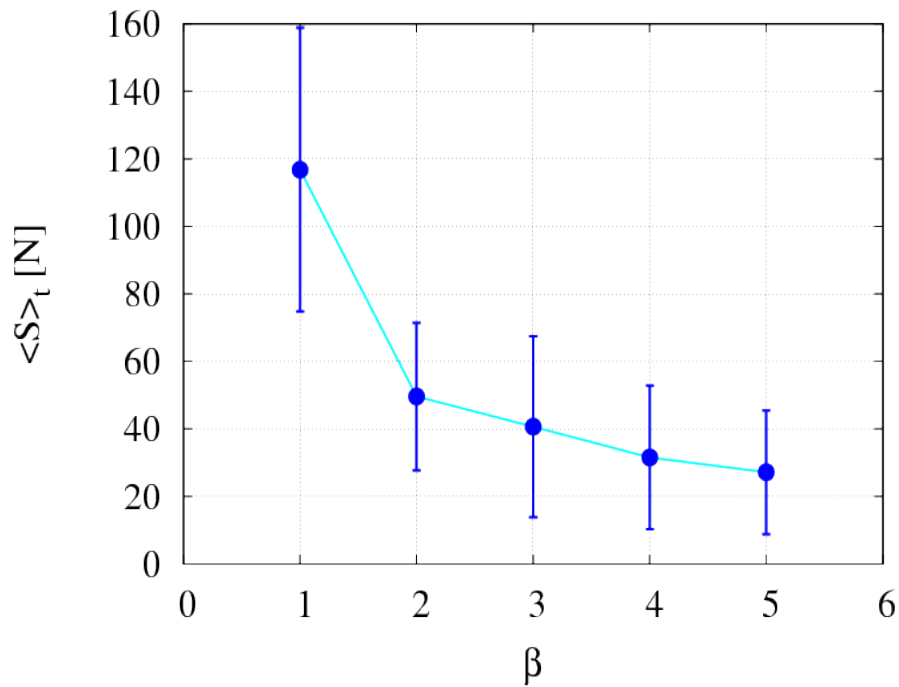
Is it possible to leave the crowd?

- Once S exceeds some predefined threshold S_c at one of the pedestrians i , the social force exerted by this pedestrian on the others is modified: $A'_i = \beta * A_i$.



- The psychological interaction of pedestrian i forced the others to withdraw, S acting on him decreases.

Is it possible to leave the crowd?



- The average sum of forces decreases with β .
- The rate of this change decreases with β , as well.

Thrown out against one's will?



- Pedestrians cross the exit one by one. If density is large enough, it's impossible to move with respect to our neighbors.
- **Can one withdraw from the crowd or she/he will be thrown out through the exit against her/his will?**

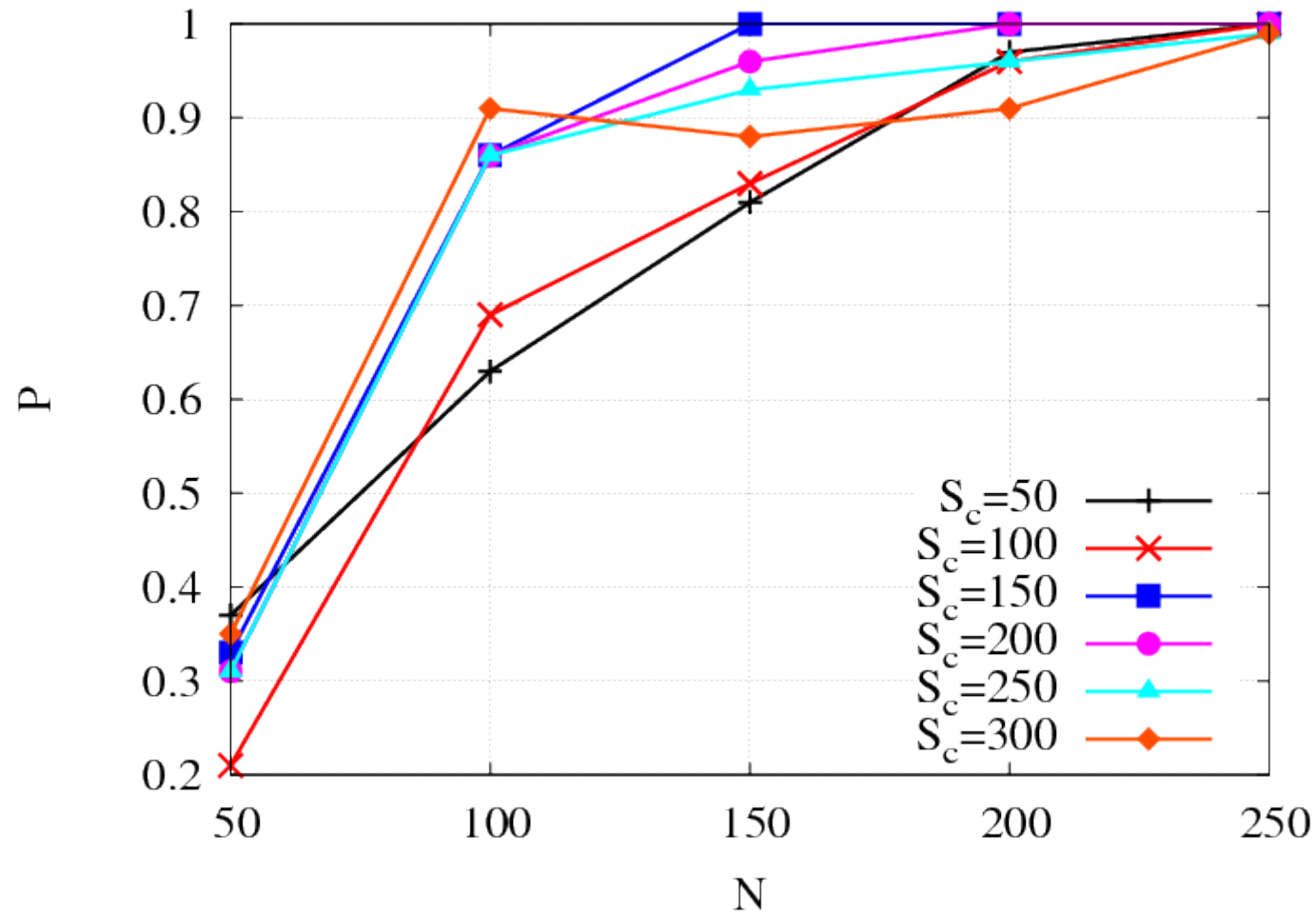
Thrown out against one's will?

- Pedestrians, numbered by $i=1, \dots, N$, are going to leave a room through a small exit.
- The sum S_i of compressive mechanical forces acting on each individual i is registered during the motion.
- Once for individual X the sum S_x exceeds the threshold value S_c , the direction of the desired motion of this individual is reverted.
- K nearest neighbors of i -th pedestrian decide to accompany her/him.
- The desired direction of K individuals, who are closest to X , when the threshold S_c is exceeded is now equal desired direction of X . The repulsive psychological force between X and her/his neighbors is attractive now.

Thrown out against one's will?

- The group of $K+1$ individuals tries to evade the exit, as if they tried to help a victim of the interpersonal forces in the crowd.
- The outcome of the simulation is the probability P , that the crowd throws X out through the exit, despite her/his struggling to withdraw from the crowd.
- If X crosses the exit despite this change of her/his intention, we call the crowd '*jammed*'.

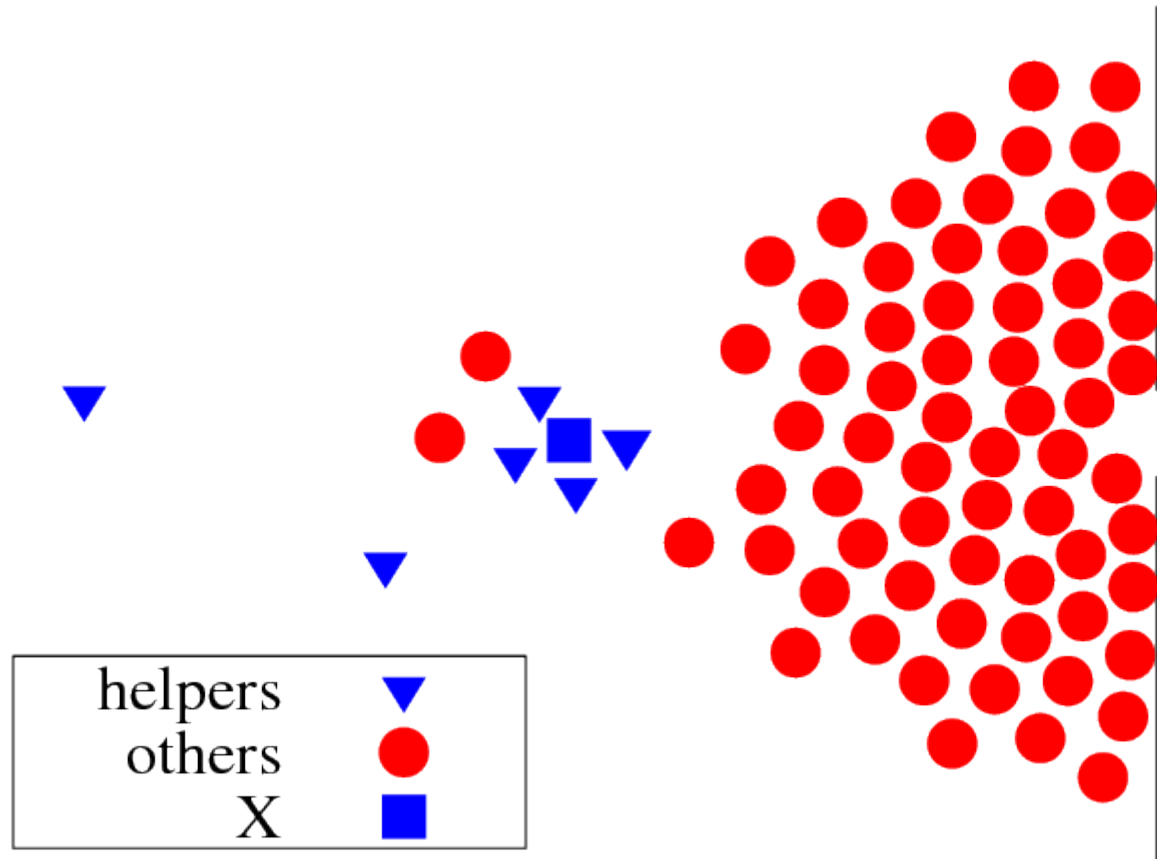
Thrown out against one's will?



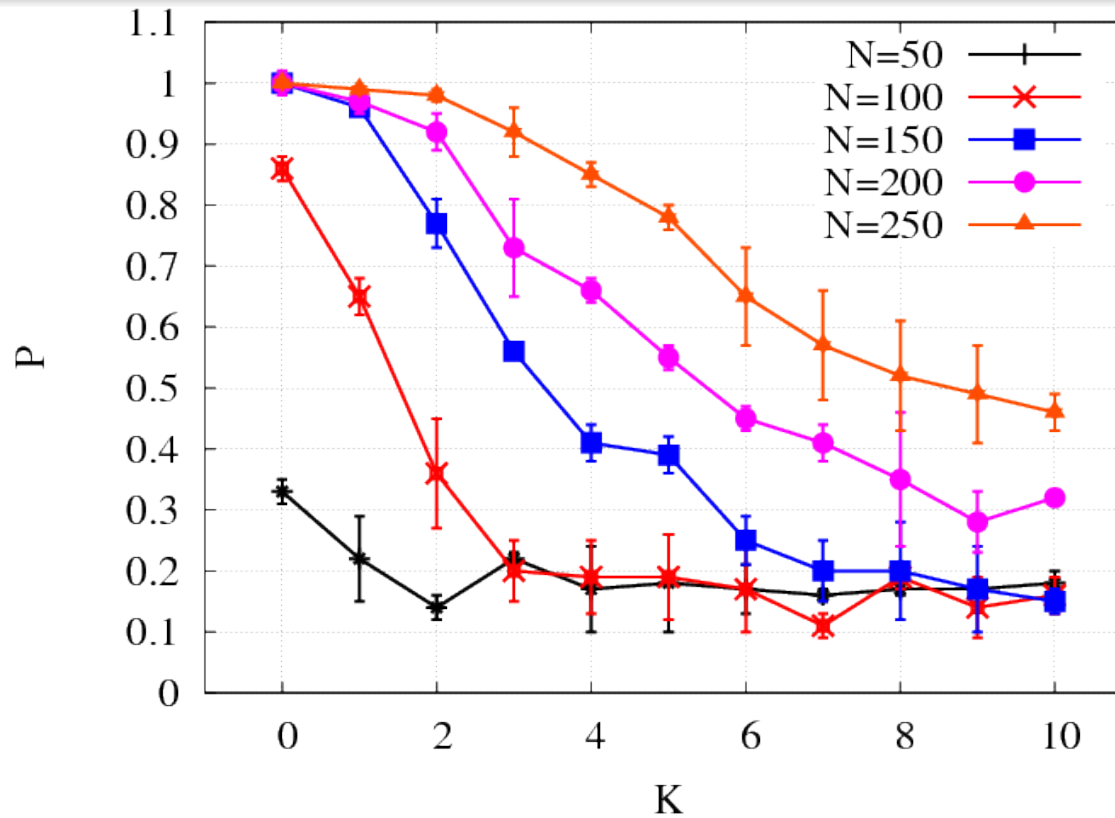
- $K = 0$ (no helpers). Average over 70 samples.
- The probability P weakly depends on S_c . The crowd size N is decisive.

Does collective action help?

- A successful help. A spatial configuration of individuals near the exit.

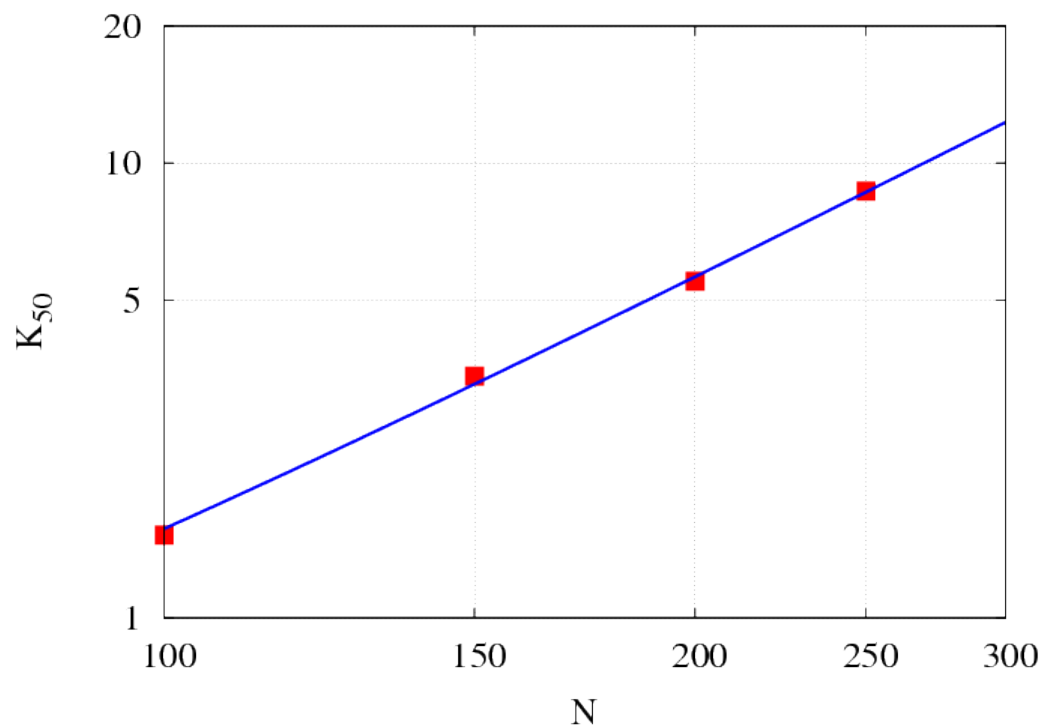


Does collective action help?



- Crowd size N is relevant, but can be to some extent neutralized by the number of helpers.
- For example, P close to 0.5 can be achieved in a crowd of $N = 100$ pedestrians with K about 2 helpers, in a crowd of $N = 200$ pedestrians with K about 5 helpers and so on.

Does collective action help?

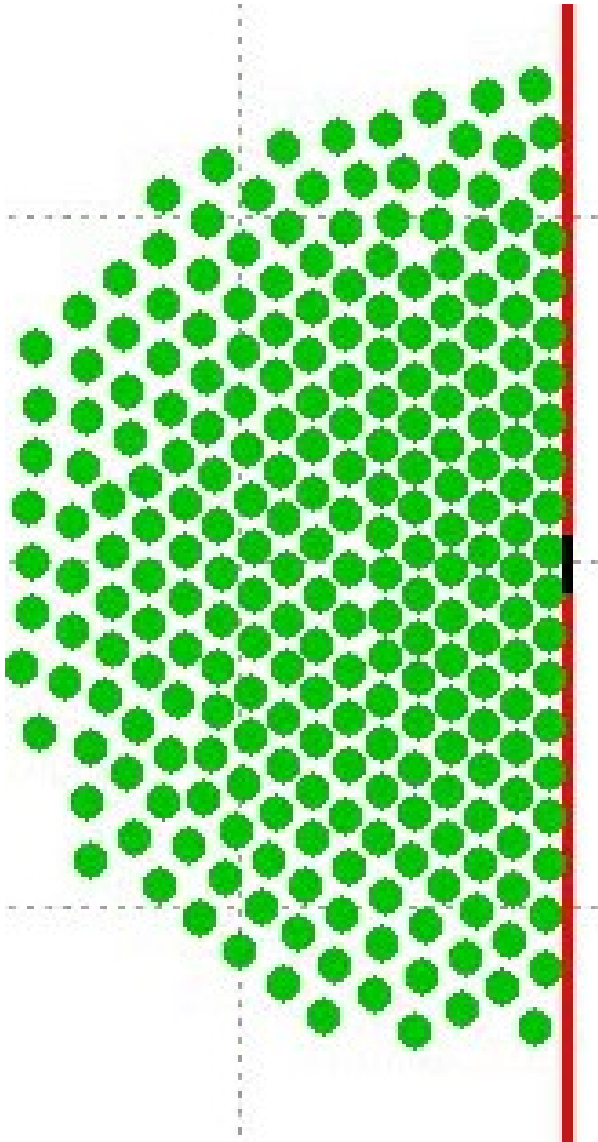


- How many helpers must be found to have a chance of 50% to withdraw from the crowd?

$$\mathbf{K_{50} \propto N^{\beta}, \beta = 1.88 \pm 0.05}$$

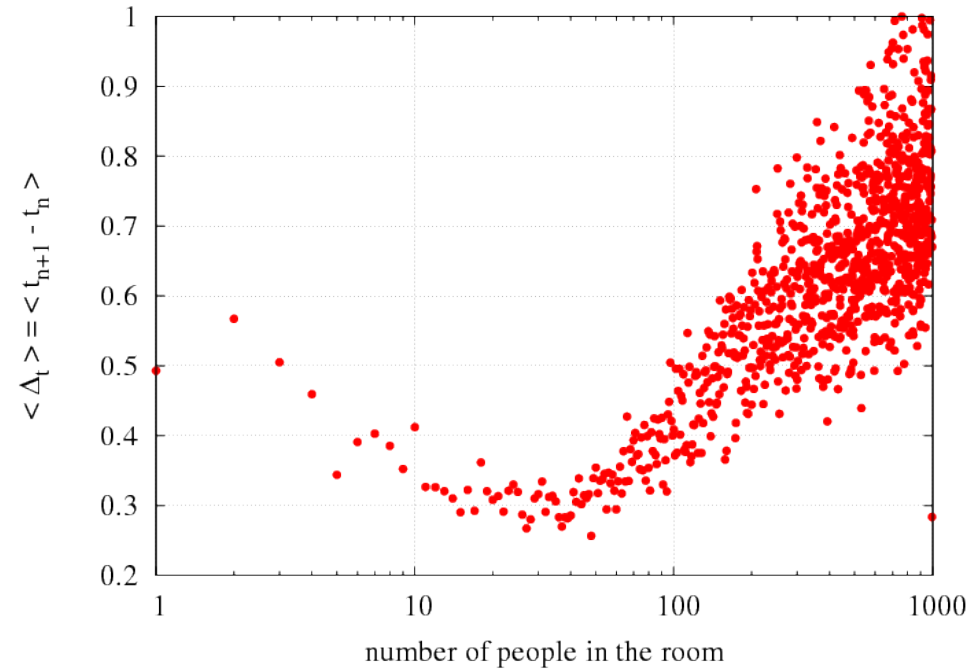
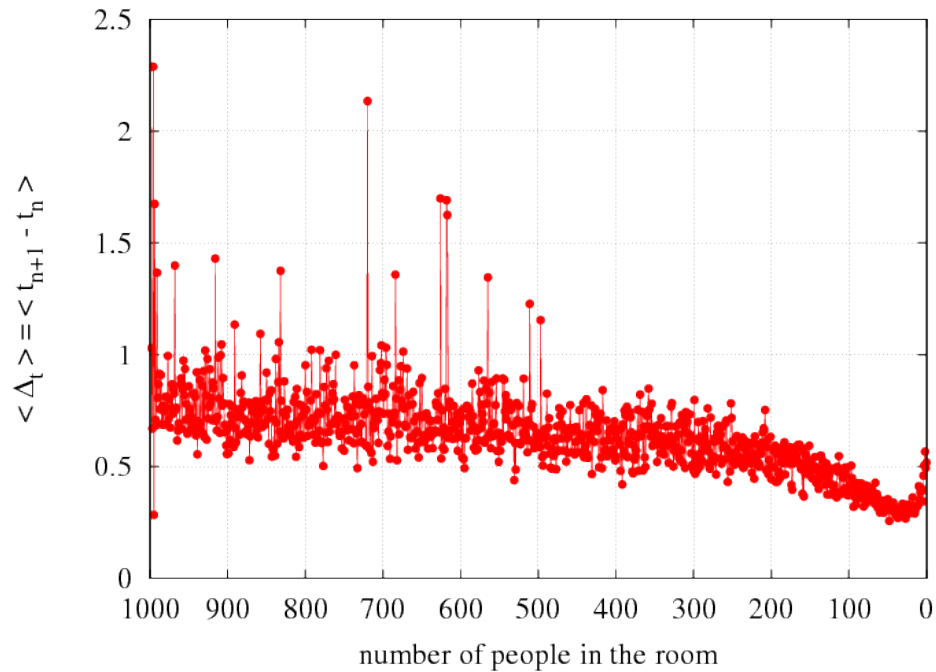
- However, as K_{50} cannot be greater than N , this behavior must end with some crossover for larger N .

A closed door scenario.



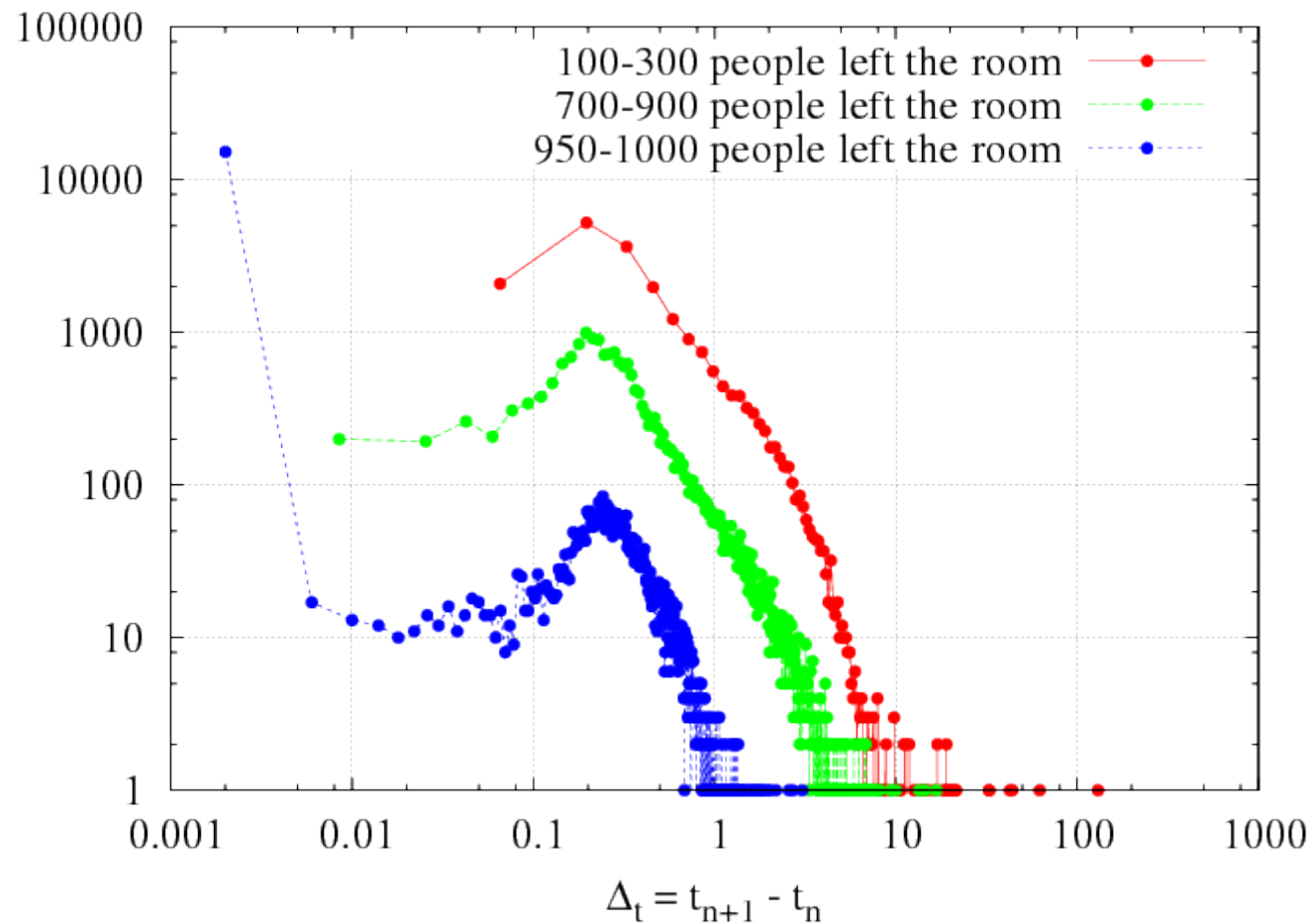
- $N=1000$ persons in a room with a small exit.
- At the initial state the door is closed and the people are crowded.
- When the crowd is formed we open the door, and we register the time at which each individual leaves the room.
- Time lags $\Delta_t = t_{n+1} - t_n$

A closed door scenario: 2 phases in the evacuation process



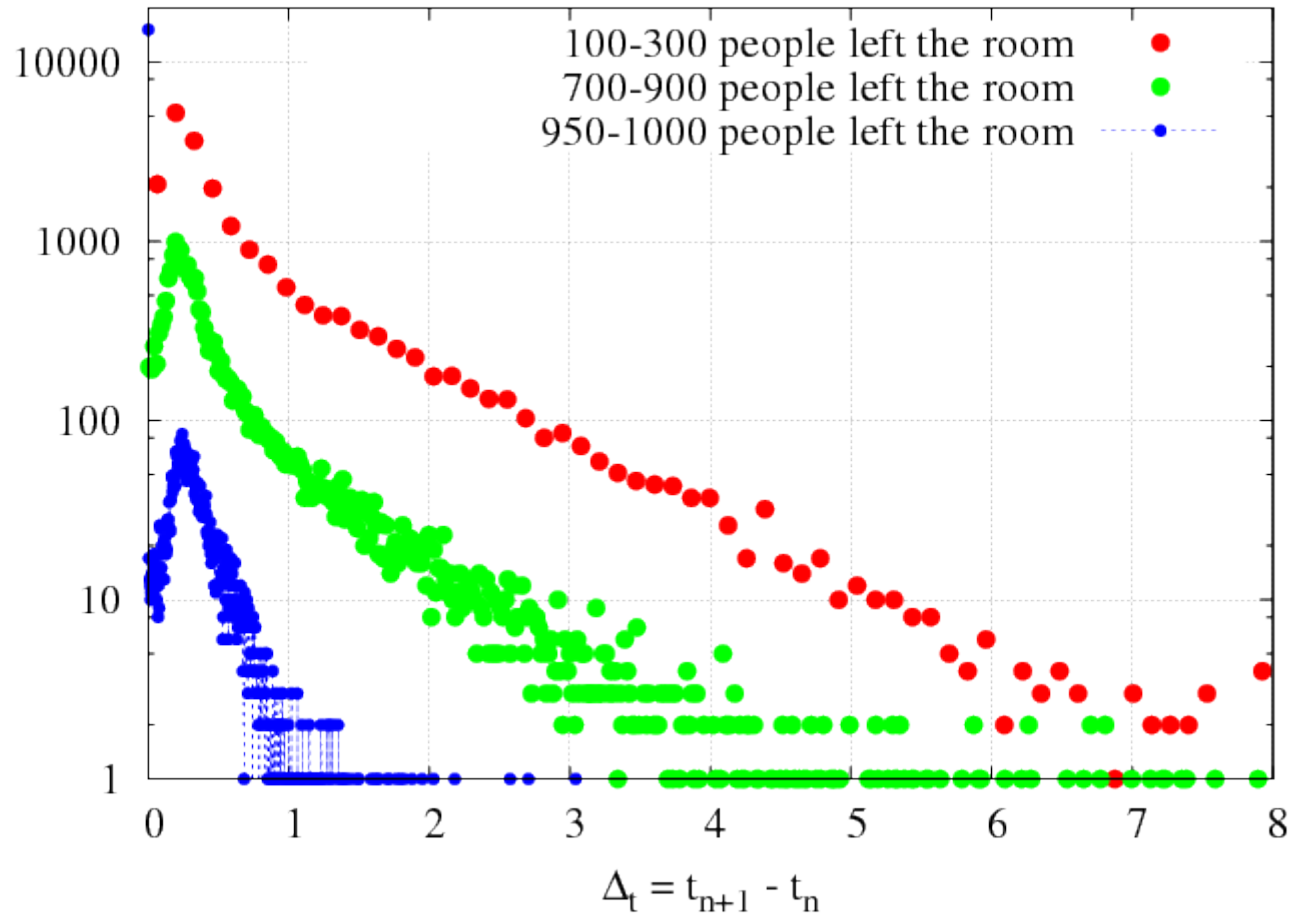
- Initially the mean length of the time lags decreases with the number of people in the room, then increases.

A closed door scenario: two characteristic times



I. Mean time interval between the exit events in a group of people leaving the room: $0.2s$.

A closed door scenario: two characteristic times



II. Clogging time $\propto e^{-\text{const } t}$

The events of clogging of the group of people are independent.

Conclusions

- Our numerical results indicate that once the crowd size N exceeds *150-200* pedestrians, it is unlikely that a single individual can withdraw under one's own steam.
- The only way then is to mobilize a group of pedestrians nearby who are willing to help. Still, the necessary number of helpers increases with the size of the crowd.
- The analysis of the time intervals between the persons leaving the room shows the correlation within a group of people leaving the room and no correlation between separate groups leaving the room.

Thank you for your attention.